# gTheoryShiny: An online application for interactive G-theory inference

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# Introduction

gTheoryShiny is an R/Shiny application for interactive construction, and inference of generalizability theory (also named G-theory) for performance assessment, which provide friendly GUI for users lacking of programming skills. It's heavely based on **lme4** (Bates et al., 2015) for multilevel modeling. To illustrate the functionality of this app, this manual is organized as following:

- Input section
  - 1. Individual Data (.csv)
- Facet screening
- Data Analysis
  - 1. g-study estimation and bootstrapping error
  - 2. d-study estimation and bootstrapping error

### Input section

#### 1. Individual Data (.csv)

Currently, the app also support .csv file. The data supported by gTheoryShiny can be either long-format or wide-format.

#### Wide-format data

If your data is wide-format, the app can help you transform the wide-format data into the long-format data. First, please make sure the first several rows of data include identifier of all facets (in the example table below, facets are *task1/task2* and *rater1/rater2*). Header is optional. If the data contains the header, check the box of *include header*. The first column of the data should be subject ID (*Person* in the table). Then, each row should represent each subject's all observations.

In addition, there are three settings you should fill in: (1) how many rows represent tag/ID, (2) the pre-fix of tag/ID, (3) column names of tag/ID in the transformed long-format data. For example, to transform table 1 to table 2, setting 1 is 2 (first two rows contains all facets' identifier), setting 2 can be T;R (the identifiers of facets have pre-fix T and R with the same order with the order of each facet's rows), and setting 3 can be Task;Rater (in long-format, the column names of facets are Task and Rater in order).

It should also be noted that the long-format data transformed in this way automate generate two columns in the first column and the last column respectively: *ID* and *Score*. ID's values correspond to subject ID, and Score's values are same as values in the corresponding cells in wide-format data. Currently, there's no way to change the column names of these two variables.

Finally, don't forget to click *Transform* button to finish the wide-to-long transformation.

Person	Task1.Rater1	Task1.Rater2	Task2.Rater1	Col5
	Task1 Rater1	Task1 Rater2	Task2 Rater1	Task2 Rater2
1	5	6	7	8

Tabl	le	1:	An	Examp	le o	f V	Vic	le-i	format	Data
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Table 2: An Example of Long-format Da
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Task	Rater	Score
T_Task1	R_Rater1	5
$T_Task1$	$R_Rater2$	6
$T_Task2$	$R_Rater1$	7
$T_Task2$	$R_Rater2$	8
	Task T_Task1 T_Task1 T_Task2 T_Task2	TaskRaterT_Task1R_Rater1T_Task2R_Rater1T_Task2R_Rater2

#### Long-format Data

If the data is already long-format before uploading, there are no extra step to set up. As figure 1 shows, only things needed to be checked are (1) check *long-format* check box under the Data

property, (2) check or un-check *include header* dependending on whether the data has headers or not.

Choose CSV File: Upload Brennan.3.2Long.cs	Raw I	Raw Data: Show 10 \$ entries			Search:		
Upload complete		Task 🍦	Person 🔶	Rater 🔷	Score 🔶		
Notice: If data is wide-format, make	1	1	1	1	5		
file should be TAG/ID, first column should be subject ID	2	1	2	1	9		
Data property:	3	1	3	1	3		
Iong-format	4	1	4	1	7		
include header	5	1	5	1	9		
	6	1	6	1	3		
	7	1	7	1	7		
	8	1	8	1	5		
	9	1	9	1	9		
	10	1	10	1	4		
	Showing 1 to	o 10 of 120 entries Previous	1 2 3	4 5	12 Next		

Figure 1: Long-format data input

# **Facet Screening**

The facet screening is second step for g-theory data analysis. When data is long-format, users should specify which column corresponds to (1) ID, (2) facets, or (3) outcome. Then two tables will pop up: (1) Structural table, which represents the relations between facets (nested or crossed), and (2) Summary table, which includes the sample size for each condition (all combination of facets).

Figure 2 shows an example of facet screening setup. Select *Person* as ID, then check *Task* and *Rater* as facets, finally select *Score* as outcome. In Structural table, it shows that *Task* and *Rater* are nested in this example.

Control facets/outcome: Which column represents ID:	Structural Ta Show 10 \$ e	ble: ntries	A North	Search:
		<b>₹ 12</b>	Nest	edOrCrossed
Which column(s) represent facets:	1 Tasl	k Rate	er Neste	d
✓ Task	Showing 1 to 1 c	of 1 entries		Previous 1 Next
Person	e			
Rater	Summary Ta	ble:		
Score Score	Show 10 🗘 e	ntries		Search:
Which column represents outcome:		Task 🔷	Rater	Sample Size (Outcome) 崇
Score 👻	1	1	1	5
confirm	2	1	2	7
	3	1	3	6
	4	1	4	4
	5	2	5	4
	6	2	6	5
	7	2	7	4
	8	2	8	4
	9	3	9	6
	10	3	10	5
	Showing 1 to 10	of 12 entries		Previous 1 2 Next

Figure 2: Facet screening setup

# **Data Analysis**

After users finish facet screening, recommended formula is automate generated in Data Analysis tab page. Figure 3 shows an example of g-thoery estimation setup. The formula follows multilevel modeling formula. The left hand side of equal sign represents the outcome. The right hand side contains the linear combination of facets and ID. For example,

$$Y = PersonID + Facet1 : Facet2 + Facet2 + Facet3$$

where Facet1 is nested within Facet2, Facet2 and Facet 3 are crossed, and PersonID denotes subject ID.

Users are allows to specify their own formula for g-theory estimation following the same format as above.

*Link Function* option allows users to specify the relation between outcome and linear combination of facets. Possible choices include identity, logit, probit, possison etc. Currently, only identity is supported.

*Number of bootstrap* allows users to specify how many bootstrapping iterations for bootstrapping measurement error estimation. The default is 200.

G-theory Data Explorer	Tutorial Data Input	Data Structure	Data Analysis	
Recommended formula:	G-study Ou	tput:		
Score = Person + Task + Person:Task + Rater:Task <b>User-specified formula:</b>	Sour 1 Person:Ta 2 Rater:Ta	ce Est.Variance sk 0.5596 sk 0.6475	Percent.Varianc 12.8 14.8	e %
Default: recommeded formula	3 Pers 4 Ta	on 0.4730 sk 0.3253	10.8	%
Link Function:	5 Residu	al 2.3803	54.3	%
identity -				
Number of bootstrap				
G-study:				
gstudy estimate				
bootstrap estimate				
Process 100% 100 / 100%	100			
<ul> <li>▲ Download theta estimates</li> <li>▲ Download gstudy result</li> </ul>				

Figure 3: Screenshot of g-theory estimation

### 1. G-theory estimation and bootstrapping

Clicking *gstudy estimate* button will provide the g-study results including sources of variance components, the estimates of variance, and percent of each variance component.

Then, as shown in Figure 4, users can click *bootstrap estimate* button to generate bootstrapping standard deviation of g-study results. All results of g-study are downloadable.

Recommended formula:	G-study Output:			
Score = Person + Task +	Source Est	Variance Perce	ent.Variance	
Person:Task + Rater:Task	1 Person:Task	0.5596	12.8%	
User-specified formula:	2 Rater:Task	0.6475	14.8%	
Defeuilte meen men de difermende	3 Person	0.4730	10.8%	
Default: recommeded formula	4 Task	0.3253	7.4%	
Link Function:	5 Residual	2.3803	54.3%	
identity -	Estimate Bootstr	apping SD for	G-study:	
	Source Est	.Variance Perce	ent.Variance 2.5% 97.5%	
Number of bootstrap	1 Person:Task	0.5596	12.8% 0.0000000 1.350828	
200 1,000	2 Rater:Task	0.6475	14.8% 0.0162325 1.534110	
	3 Person	0.4730	10.8% 0.0000000 1.337575	
100 190 280 370 460 550 640 730 820 910 1,000	4 Task	0.3253	7.4% 0.0000000 2.354895	
G-study:		2.3003	J4. J7 1./22/0JU J.U/1122	
a-study.				
astudy estimate				
gotady commute				
bootstrap estimate				
Process 100% 100 / 100				
100%				
▲ Download theta estimates				
🕹 Download gstudy result				
🛓 Download bootstrap result				

Figure 4: Screenshot of bootstrap estimation

#### 2. D-study estimation and bootstrapping

To get results of D-study, users need to select (1) which facet to change, (2) how many potential levels of facets. Users can change other facet by repeating these two steps, then click *confirm* facet levels button. For example, the figure below shows facet Task is set up to 60 level in D-study.

After settings of d-study are finished, clicking *dstudy estimate* will provide the results of dstudy, which contains two parts: levels of facets in D-study and statistics of d-study. Figure 6 shows an example of d-study with there are 60 tasks in d-study.

Similiar to G-study, to get boostrapping SD of d-study, click *bootstrap estimate* button. Finally, click *download* button to download results of D-study.

D-study:	
Select the facet to cha	ange
Task	-
level:	100
0 10 20 30 40 50 60	70 80 90 100
confirm facet levels	

Figure 5: Screenshot of D-study settings

# D-study Output:

Sample Size:

Task Rater 60 12

Result:

```
The generalizability coefficient is: 0.9739873.
The dependability coefficient is: 0.9614728.
The relative error is: 0.01263264.
The absolute error is: 0.01895361.
.
      Source Est.Variance
                            N Est.(Var/N)
1 Person:Task
                   0.5596 60 0.0093266667
  Rater:Task
2
                   0.6475 720 0.0008993056
3
      Person
                   0.4730 120 0.4730000000
4
        Task
                   0.3253 60 0.0054216667
5
    Residual
                   2.3803 720 0.0033059722
```

Figure 6: Screenshot of D-study output